Adaptive metalenses with simultaneous electrical control of focal length, astigmatism, and shift

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Focal adjustment and zooming are universal features of cameras and advanced optical systems. Such tuning is usually performed longitudinally along the optical axis by mechanical or electrical control of focal length. However, the recent advent of ultrathin planar lenses based on metasurfaces (metalenses), which opens the door to future drastic miniaturization of mobile devices such as cell phones and wearable displays, mandates fundamentally different forms of tuning based on lateral motion rather than longitudinal motion. Theory shows that the strain field of a metalens substrate can be directly mapped into the outgoing optical wavefront to achieve large diffraction-limited focal length tuning and control of aberrations. We demonstrate electrically tunable large-area metalenses controlled by artificial muscles capable of simultaneously performing focal length tuning (>100%) as well as on-the-fly astigmatism and image shift corrections, which until now were only possible in electron optics. The device thickness is only 30 μm. Our results demonstrate the possibility of future optical microscopes that fully operate electronically, as well as compact optical systems that use the principles of adaptive optics to correct many orders of aberrations simultaneously.

INTRODUCTION

There has been a wide variety of work on tunable optical devices, particularly tunable focus lenses (that is, varifocal lenses), with important applications in imaging and adaptive vision. Focus tuning is usually performed by the mechanical movement of rigid elements (1), which provides great imaging performance at the expense of bulk and inertially limited speed. Other applications include liquid crystal-based spatial light modulators (2–4), which can be relatively high speed and capable of correcting for aberrations but are limited in resolution and polarization dependence; fluid-based tunable lenses (5–10) (including those incorporating elastomeric materials), which can be high speed, have a wide tuning range, and are relevant for small-scale devices but whose exact surface curvature is difficult to control (for example, coma is observed when the lens is placed vertically, as a result of gravity); tunable acoustic gradient index lenses (11), which can be tuned at high speeds but must be used stroboscopically; and electro-optic lenses (12), which are high speed but polarization-sensitive. In astronomy (13, 14) and microscopy (15), adaptive optics uses deformable mirrors to correct for wavefront distortions but must operate in reflection.

Recently, flat lens technology based on metasurfaces (16), which control the wavefront of light using subwavelength-spaced nanostructures, has shown considerable potential in optical performance while reducing element thickness to the micrometer level, opening up new opportunities to replace bulk optical devices with thin, flat, lightweight devices (17, 18). Instead of moving several optical components longitudinally along the optical axis as in telephoto lenses and autofocus cameras, in metasurfaces, lateral control can be used to vary focus and magnification, as well as other adaptive optics capabilities (13–15), and to leverage their flatness. Reported recently were mechanically tunable metasurfaces in which metasurfaces were embedded in stretchable substrates (19–21) but were limited in size (less than a millimeter in diameter), required external apparatuses to apply strain, and had inherent speed limitations, restricting their applications. In addition, no theoretical analysis of the effect of strain field tuning on optical aberrations was presented. Here, the combination of metasurface optics and dielectric elastomer actuators (DEAs)—sometimes referred to as artificial muscles (22) in soft robotics—offers a versatile platform for electrically tunable optical devices through the design of phase, amplitude, and polarization profiles.

A flat lens can be constructed by a metasurface with the following hyperboloidal phase profile (17)

$$\phi(r) = \pm k \left( \sqrt{r^2 + f^2} - f \right)$$

where \(k\) is the wave number, \(r\) is the radial position, \(f\) is the focal length, and the positive or negative sign is applied for diverging or converging lenses, respectively (Fig. 1A). A lens described by Eq. 1 focuses light that is free of spherical aberrations for normal incidence (infinity-corrected) illumination. By combining this metasurface with a DEA, the lens can be made electrically tunable.

A DEA (22), which is a type of electroactive polymer, is effectively a compliant parallel plate capacitor that stretches when a voltage or electrical field is applied (23). By using a soft elastomer (for example, polyacrylate and silicone rubber) as a dielectric, together with transparent, stretchable electrodes (5), the configuration is slightly compressed in the thickness direction when a voltage is applied. As elastomers conserve volume on deformation, thinning results in a lateral expansion that can be very large (~500%) (24). The attainable actuation strain is a function of the electrostatically induced Maxwell stress, the constitutive deformation behavior of the elastomers, and the mechanical configuration of the elastomers and electrodes (25). Bonding a metasurface with the DEA couples the metasurface profile to voltage-induced stretching, which is approximately uniform over a single electrode area. Effectively, the coordinates of the metasurface scale by a stretch factor, \(s = 1 + \varepsilon_L\), where \(\varepsilon_L\) is lateral strain, such that \(r \rightarrow r/s\)

$$\phi_{\text{stretched}}(r, s) = \pm k \left( \sqrt{(r/s)^2 + f_0^2} - f_0 \right)$$

where \(f_0\) is the focal length without actuation (Fig. 1B). The focal length of Eq. 2 varies quadratically with stretch: \(f(s) = s^2 f_0\) (see
Materials and Methods). The voltage dependence of the focal length provided by the DEA is

$$\frac{f}{f_0} = \frac{1}{1 - (\varepsilon / Y)(V / t)^2} \tag{3}$$

where $V$ is the voltage and $\varepsilon$, $Y$, and $t$ are the permittivity, Young’s modulus, and dielectric layer thickness, respectively. Tuning in this manner introduces negligible aberrations (fig. S1; see also Materials and Methods).

In practice, an infinite number of wavefront aberrations can exist and can be quantified in terms of Zernike polynomials (table S1). In most cases, the eight lowest terms are sufficient: piston, tip, tilt, defocus, oblique and vertical astigmatism, and vertical and horizontal coma. Because the Zernike terms are linear and orthogonal, specific aberrations can be targeted and tuned by introducing the appropriate displacement field to the phase profile. In general, applying the stress of a particular configuration induces a strain field, resulting in a displacement field. The displacement field can be regarded as the sum of deformation ($A$) and rigid-body displacement ($B$) components, in which the transformed coordinates can be expressed as follows: $x' = A(x, \eta) + B(\eta)$, where $\eta$ is a parameter (for example, voltage) and $x$ and $x'$ are the original and transformed coordinates, respectively (26). For metasurfaces, the phase profile transforms as $\phi(x, y) \rightarrow \phi(x', y')$. The rigid-body displacement is simply a lateral shift of the entire phase profile, whereas the deformation changes the shape or size, resulting in a shape change of the passing wavefront. In the case of asymmetric biaxial strain, the coordinates of the phase profile transform as $(x, y) \rightarrow (x/s_x, y/s_y)$: $\phi = \pm k \left( \sqrt{(x/s_x)^2 + (y/s_y)^2 + f^2 - f_0} \right)$, where $s_x \neq s_y$. Light propagating along two perpendicular planes experiences different focal lengths, which is astigmatism. Thus, through an electrically controlled strain field, it is possible to create the optical analog of image shift and stigmators (Fig. 1, C and D) found in electron microscopes (27).

**RESULTS**

**Adaptive metasens design**

A polarization-insensitive, converging metalens [diameter (ø) = 6 mm, $f = 50$ mm, $\lambda = 1550$ nm; see Fig. 2A] was combined with a DEA constructed using transparent polyacrylate elastomers with transparent, stretchable patterned electrodes made of single-walled carbon nanotubes (SWCNTs) (figs. S2 and S3; see also Materials and Methods) (28). The DEA was measured to exhibit large transparency windows in the visible, near-infrared, and mid-infrared spectra (fig. S4). Focal length tuning was implemented by applying a voltage through the center electrode $V_5$ to increase focal length or from $V_1$ through $V_4$ to decrease focal length (Figs. 1B and 2), corresponding to lateral expansion or contraction of post spacings, respectively. Control of vertical astigmatism in the $x$,$y$ directions (“$x$,$y$ stigmators”) was implemented by activating opposing pairs of electrodes (Figs. 1C and 2). Image shift was implemented by activating one peripheral electrode, $V_1$ through $V_4$, such that its expansion caused the entire metasurface to shift in space (Figs. 1D and 2). Any combination of actuations, each implemented using different voltages, was also possible (fig. S5).

Two types of devices were fabricated and measured: a single-layer (SL) device and a double-layer (DL) device (fig. S5A). Although the SL
device demonstrated better tunability compared to the DL device [for the same applied voltage, the SL device was stretched more than the DL device on account of the lesser stiffness introduced by the smaller intermediate elastomer layer (IEL)], most of the data presented were those of the DL device because of its higher quality. The maximum voltage used was 3 kV, producing $s = 1.41$ (SL) and $s = 1.15$ (DL) (Fig. 3).

**Focus measurement**

Focal length was measured by scanning a camera along the $z$ axis for varying voltages (Fig. S6). From $f_0 = 50 \text{ mm}$, the DL focal length was tuned by 15 mm ($Af/f_0 = 30\%$) with 3 kV (Fig. 3C) and closely followed the predicted voltage relation (Eq. 3 and fig. S7), whereas the SL device exhibited greater (107%) focal length modulation (Fig. 3C, inset). The focusing efficiency (DL), defined as the ratio of focused optical power to incident power (fig. S6C), showed a high average efficiency of 62.5% with little variation throughout the tuning range (Fig. 3B). The near-constant efficiency was due to the relatively small stretching range used, which allowed the posts to maintain subwavelength spacing, and to the high optical confinement factor (the calculated confinement factor, defined as $\Gamma = P_{\text{inside post}}/P_{\text{total}}$) of 0.71 ± 0.01 and 0.69 ± 0.01 for $s = 1$ and $s = 1.09$, respectively) within the posts as a result of the large index contrast (29), which minimized the effect of changes in gap size. At 0 and 1 kV, focal spot sizes ($1/e^2$ full beam waist) were measured and compared to the theoretical diffraction-limited spot sizes ($\sigma = 6 \text{ mm}$, $M^2 = 1.3$): $34.4 \pm 1.1 \mu\text{m}$ (diffraction limit, $21.4 \mu\text{m}$) and $37.7 \pm 2.8 \mu\text{m}$ (diffraction limit, $22.7 \mu\text{m}$), respectively (Fig. 3A). Possible explanations for these differences included fabrication errors and small distortions introduced when the elastomer was initially pressed onto the metasurface. Because of setup constraints, images of the focal spots at higher voltages (>1 kV) were obtained directly by the camera without magnification (Fig. 3B).

**Stigmatator and shifter measurement**

The effect of the $x$ stigmatator, which squeezed the phase profile into an elliptical shape, was measured to show asymmetric yet spatially uniform biaxial strain according to FT images (Fig. 2B), indicating good stigmatator performance corroborated by the Zernike transform (Fig. 3D). The sharpness of the FTs is indicative of the quality of the lenses, whereas the radii of the first-order annulus, corresponding to the reciprocal space representation of the radial periodicity between posts, are a measure of the biaxial stretch. The features seen in the FTs are signatures of symmetries used by the metasurface design algorithm.

The $x,y$ shifters were able to shift the image in all cardinal directions by applying appropriate control voltages (Fig. 3E). The observed control asymmetry was likely due to residual asymmetric stiffness around the periphery of the device because three different structures needed to be concentrically aligned during fabrication: the outer frame, the electrodes, and the metasurface. Shift-induced distortions of the metasurface were minimal (fig. S8).

**Reliability test**

The reliability of the device was tested with a sinusoidal voltage from 2 to 100 Hz at an amplitude of 2.5 kV (movie S1). The device did not fail, nor was image quality observed to degrade after >1000 cycles. The mechanical robustness of the device was attributed to the relatively small actuation strains applied. By applying a voltage square wave, the response time was measured to be 33 ± 3 ms (fig. S9) and was mainly limited by the elastomer viscoelasticity, charge transfer, and dissipation time in SWCNT electrodes. Dielectric breakdown was measured at ~3.5 kV, when the current began to flow through the dielectric, damaging the device. The electrical breakdown was a “soft” breakdown associated with local burning through the elastomer, and the same devices were able to resume operation after cycling power. This self-healing feature was attributed to the burning and subsequent clearing of SWCNT electrodes around the breakdown location, which prevented further electrical shorting.

**DISCUSSION**

We have demonstrated an electrically tunable metalens with multiple, simultaneous control parameters, as well as a centimeter-scale metalens. In comparison to existing systems, our device offers a route to extremely compact, lightweight transmissive adaptive optics with large, well-controlled tunability and high-definition (subwavelength) phase profiles. It is capable of performing focus tuning and aberration control simultaneously. In its current form, it is limited in speed and requires a high operating voltage. We note that our demonstration of astigmatism and image shift tuning is important for the correction of misalignment in optical systems based on metasurfaces. By using thinner elastomers (30) (operating voltage <12 V) or miniature high-voltage components
that are commonly found in devices such as mobile phones (for example, flash modules), voltage requirements may be substantially reduced. Speed may be further increased to the microsecond time scale \((31)\). Custom-made elastomers such as silicone-based elastomers \((30)\) could provide a direct path for these improvements because elastomer dimensions and electromechanical properties could be tailored during processing. However, in addition to the mechanical stability of devices, the use of thinner or different elastomers requires adaptation and optimization of other aspects, such as the choice of stretchable electrodes and the lens transfer process. Devices can be made using the same method, with diameters ranging from micrometers to centimeters. These desirable characteristics are suitable for integration in size- and weight-limited imaging systems and wearable devices. Our results demonstrate the feasibility of embedded autofocus, optical zoom, image stabilization, and adaptive optics, which are expected to become essential for future chip-scale image sensors and head-mounted optics such as those found in stretchable electronic eye camera sensors \((32)\), providing possibilities for new kinds of imaging systems.

**MATERIALS AND METHODS**

**Experimental design**

**Metalens design**

The unit cell of the design is shown in fig. S3A. The height \((h)\) of the posts was 950 nm. By varying the diameter of the posts \((d = 810 \text{ to } 990 \text{ nm})\), a phase coverage of close to \(2\pi\) and a high uniform transmission amplitude response were achieved (fig. S3B). These data were used as a lookup table to digitize the phase profile. Post diameters with low transmission values (for example, \(d = 860 \text{ and } 870 \text{ nm}\)) were excluded from the lookup table. Given the circular shape of the post structures, the phase and amplitude responses were independent of the polarization of the incoming light. The phase profile was realized using subwavelength antennas with fixed edge-to-edge separation (fig. S3C), by which the placement of antennas was made denser than that with conventional fixed center-to-center separation. Hence, the size of the unit cell \((a)\) was equal to the sum of the
post diameter \((d)\) and the constant edge-to-edge spacing \((e)\): \(u = d + e\). In our design, we chose the edge-to-edge spacing to be 650 nm, which was determined by the feature size of the stepper used and the length scale to avoid interaction between neighboring antennas. 

**Selection of Materials**

A wide range of elastomers with varying chemical, mechanical, and dielectric properties have been reported for electrostatic actuation (22). We chose an off-the-shelf acrylate elastomer \([VHB\ Tape\ 4905\ (hereafter\ referred\ to\ as\ VHB),\ 3M]\) because it was transparent, sticky, easily available, and capable of handling large strain (33). Although there were limited choices for VHB thickness and VHB was not purposely optimized for DEA applications, the use of VHB provided a balance between ease of preparation and optical/actuation performance. Silicone-based elastomers, which are also transparent, offer more precisely optimized for DEA applications, the use of VHB provided a balance between ease of preparation and optical/actuation performance.

Silicone-based elastomers, which are also transparent, offer more precise control, greater temperature stability, and very low hysteresis, but their use requires additional processing steps.

Transparent, stretchable electrodes were prepared from SWCNTs. A controlled, uniform distribution of SWCNT mats was achieved using a water-based SWCNT dispersion and filtration method. This method produced SWCNT mats on a polytetrafluoroethylene filter that could be directly transferred onto elastomers by pressing them and patterning them with a mask. Applications of DEAs for in-line optical devices required the optimal density of SWCNTs (28). A low density was desired to minimize the optical absorption and mechanical stiffening of the actuator. However, a higher density was needed to maintain electrical percolation (particularly for large-area actuation) and to minimize the RC (resistive-capacitive) constant.

To transfer a metasurface from its substrate to the elastomer membrane, we used a sacrificial layer. It was important for the sacrificial layer to be soluble in a solvent orthogonal to both the metasurface and the elastomer such that the solvent only dissolved the sacrificial layer but not the metasurface or the elastomer. We chose germanium dioxide (GeO\(_2\)) as the sacrificial layer because it could be readily dissolved in water. Water enables versatility in the use of the process such as in a wide variety of metasurface materials and membrane materials, as well as in other applications.

**Device Fabrication**

A film stack was first prepared for nanofabrication (fig. S2A). Starting with a silicon wafer, we deposited a 0.4-μm layer of elemental germanium (Ge) by electron beam evaporation. The sample was then placed in a furnace (Tystar Tytan) for dry oxidization in the presence of O\(_2\) at 550°C for 3 hours, which converted the layer of Ge into GeO\(_2\), completing the sacrificial layer. We found that the GeO\(_2\) layer made by dry-oxidizing Ge was significantly more soluble in water than were layers deposited by either electron evaporation or thermal evaporation directly using GeO\(_2\) as the source material, possibly due to formation of GeO\(_x\) species at high temperatures. GeO\(_2\) also dissolved much faster in water than did Ge in hydrogen peroxide (H\(_2\)O\(_2\)) and water solution, in which the rate-limiting step was the oxidation of Ge into GeO\(_2\) by H\(_2\)O\(_2\). The metasurface itself was composed of nanostrips made of amorphous silicon (a-Si) with a height of 950 nm, so a layer of a-Si with the corresponding thickness was deposited using plasma-enhanced chemical vapor deposition.

In preparation for photolithography, the sample surface was first spin-coated with the adhesion promoter hexamethyldisilazane at 4000 rpm. Next, a 1-μm layer of i-line photoresist (SPR700-1.0, DOW) was spun-coated and soft-baked at 95°C for 60 s. Over the photoresist, a layer of photobleachable contrast enhancement material (CEM365iS, Shin-Etsu MicroSi) was spun-coated at 4000 rpm to improve feature contrast for the following stepper exposure.

The metasurface design (fig. S3) was patterned into the photoresist using stepper photolithography, which allowed us to produce large-area metalenses with high yields. A quartz photomask was patterned using a high-resolution laser lithography system (DWL 2000, Heidelberg Instruments). This photomask was then used as a reticle in a 5× reduction i-line stepper (GCA AS200 AutoStep) to expose the photoresist. After exposure, the CEM365iS layer was removed by spraying deionized water (DIW) and spin drying. The sample was then postexposure-baked at 115°C for 60 s. The photoresist was then soaked in a developer (MF CD-26) for 90 s and rinsed in DIW. Mild O\(_2\) plasma descum was performed to improve pattern fidelity.

The photoresist pattern was used as an etch mask to create the metasurface in the a-Si layer. The sample was etched using an inductively coupled plasma (ICP) reactive ion etch (RIE) system (STS MPX/LPX ICP RIE), in which the etchant gases used were perfluorocyclobutane (C\(_4\)F\(_8\)) and sulfur hexafluoride (SF\(_6\)). The pattern was etched completely through the a-Si layer and as much as 100 nm into the sacrificial layer. Finally, the photoresist was removed by soaking the sample in N-methyl-2-pyrrolidone solution (Remover PG, Microchem) for 8 hours, followed by a dry resist strip in a high-temperature (200°C) and high-power (500 W) O\(_2\) plasma asher (Matrix Plasma Asher) for 20 s, leaving a-Si and GeO\(_2\) exposed (fig. S2B).

A membrane of the elastomer (VHB) was uniformly biaxially stretched (four times, linearly) and mounted by its own adhesion on a rigid circular plastic ring to create the DEA. SWCNT electrodes were then applied to either side of the membrane (~30 μm thick).

The simplest electrode configuration (single area) is a disk of SWCNTs concentrically applied to both sides of the membrane in equal areas to produce a single uniform deformation region. More complex electrode configurations were made by patterning multiple electrodes on the same membrane, for instance, by putting multiple addressable patches on one side of the membrane and a common ground electrode on the other side. We fabricated two kinds of electrode patterns: (i) a single area and (ii) a five-segment area. The five-segment device allowed for the creation and control of different strain fields, including radial expansion and contraction strains in the center, uniaxial strain in both x and y directions, and rigid-body displacements in both directions.

A mask for producing the electrode pattern was created by cutting (using a computer numerically controlled cutter) out a stencil of the desired electrode configuration in a polyethylene terephthalate film coated with nonstick silicone. This mask was first applied over the elastomer membrane. A thin, uniform layer of SWCNTs was prepared using the vacuum filtration transfer method, in which a water dispersion of SWCNTs was passed through a Teflon filter, depositing a uniform mat of SWCNTs (28). The SWCNT mat was then transferred over the mask and membrane by pressing firmly and peeling off the filter and electrode mask, leaving behind the SWCNTs adhered to the membrane.

To transfer the metasurface to the DEA, we first bonded the metasurface and a scaffold membrane (also VHB) together, after which the scaffold membrane was bonded to the DEA. We originally thought that the adhesion between the metasurface and the membrane would be enhanced by cleaning the surface with oxygen plasma treatment to expose dangling bonds in the form of reactive hydroxyl groups. However, we found that the opposite was true: The same dangling bonds also increased hydrophilicity, which allowed the presence of water or humidity to infiltrate and undercut the bonding between the metasurface and the membrane, rendering weak adhesion. Instead, pure isopropyl alcohol was used to clean the surface of the metasurface, and a chemical
adhesion promoter (AP115, 3M) was used to make the metasurface slightly hydrophobic through surface silanization. AP115 was sprayed onto the metasurface and was quickly wiped off using a lint-free cloth to reduce the contact time of the sacrificial layer with the small amount of water present in AP115. Although we did not know the exact chemical contents of AP115, the active ingredient was probably 3-glycidoxypropyltrimethoxysilane. Next, the membrane was pressed onto the metasurface, using a smooth, spherical press made of soft silicone. A spherical press was important in overcoming the nanoimprint proximity effect (34), by which there is less adhesion in the center than in the periphery when a flat press is used. The entire sample was then heated in an oven at 50°C for 3 hours to improve adhesion (by allowing the membrane polymer to flow) and then cooled to room temperature.

For release, the entire sample was immersed in water (fig. S2A). Dissolution began around the edges of the devices and moved toward the center as water slowly percolated between the nanostructures. The release time of the entire device depended on the device area and varied between minutes and hours. The scaffold membrane with the supported metasurface was then attached to the DEA by gently pressing it. We refer to the scaffold membrane after combination as the IEL. Two types of layered devices, which we refer to as SL and DL devices, were made: the SL device contained an IEL (not prestretched) that was cut to be as small as the metasurface, whereas the DL device contained an IEL (pre-stretched four times, linearly) with an area equal to the entire DEA, effectively increasing the stiffness of the combination.

In the final step, electrical contacts with the CNT electrodes were made. The SWCNT electrode patches were connected by conductive silver grease to the leads of a conductive carbon tape, which were then connected to wires.

**Measurement methods**

A tunable laser (HP 8168F) operating between 1440 and 1590 nm was used as the light source. The optical output of this laser was connected to an optical fiber collimator (Thorlabs F810APC-1550), which produced a collimated beam that was 7 mm in diameter. The collimated beam was used to illuminate the device. The polarization of the beam was allowed to wander because the device was designed to be polarization-independent, and no polarization dependence was observed. A high-voltage source (Trek 610E) was used to tune the device. After passing through the device, the light was measured by a conventional horizontal microscope setup: A microscope objective (10× Mitutoyo M Plan Apo NIR infinity corrected objective) and a tube lens (Plano-Convex Lens, f = 200 mm) were used to magnify the beam to fully visualize the focal spot on the camera (digital InGaAs, Raptor OWL640). The entire horizontal microscope setup was mounted on a linear motor (NPM Accu, line SLP35), which allowed horizontal scanning of the light field with a positional accuracy of 1 μm. This setup (fig. S6, A and B) was used to characterize focal length and focal spot size. To measure the efficiency, we replaced the microscope objective, tube lens, and camera with an optical power meter (Thorlabs PM100D) (fig. S6C). For comparison, the measured focusing efficiency of the metasurface before transfer (fabricated on a fused silica wafer) was 91%, and the difference in device efficiency was attributed to scattering and absorption by the DEA, as well as to imperfections in the transfer process.

**Uniform stretching approximation**

A lens that focuses normal incident light has the following hyperboloidal phase profile: \( \phi_{\text{ideal}} = \pm k \left( \sqrt{r^2 + (s f_0)^2} - s f_0 \right) \), where we desire a tunable focal length relationship of the form \( f = s^2 f_0 \). Achieving \( \phi_{\text{ideal}} \) requires a stretch profile that depends on the radial position \( r \), then the phase profile of a lens with focal length \( f_0 \) that is stretched by \( s \) undergoes a coordinate transformation \( r \rightarrow r/s \), such that the resulting phase profile is as follows: \( \phi_{\text{radial}} = \pm k \left( \sqrt{(r/s)^2 + (s f_0)^2} - s f_0 \right) \).

To find the stretch profile that produces the target phase profile \( \phi_{\text{ideal}} \) which has a nominal, uniform stretch value \( s \), we can equate \( \phi_{\text{radial}} = \phi_{\text{ideal}} \) and write \( s_{\text{ideal}} \) in place of \( s \) (where \( s_{\text{ideal}} \) is a specific case of \( s \) that produces \( \phi_{\text{ideal}} \)).

\[
\sqrt{(r/s)^2 + (s f_0)^2} - s f_0 = \sqrt{r^2 + (s f_0)^2} - s f_0.
\]

Solving for \( s_{\text{ideal}} \), we find the following: \( s_{\text{ideal}}(r) = r/\sqrt{r^2 + (s f_0)^2} \). To lowest order, we see that \( s_{\text{ideal}} \approx s \). Although \( s_{\text{ideal}} \) is not exactly equal to \( s \), their difference is extremely small. Figure S1 (A and B) shows that there is a slight decrease in local stretch as the radial position is moved outward from the center of the lens, using the lens parameters of our experiment (\( f_0 = 50 \) mm).

A nominal stretch of \( s = 1.2 \) yields a difference of only \( \Delta s = 1 \times 10^{-4} \) at a radial position of 3 mm, corresponding to the size of the lens in our device.

**Focal length versus voltage relation**

Volume conservation of the elastomer requires that \( s x s y s z = 1 \), where \( s \) is the stretch. For isotropic materials under uniaxial compression, \( s_x = s_y = s_z \), where \( s = 1 + e_1 \) (where \( e_1 \) is the lateral strain) and \( s_z = 1 + e_2 \) (where \( e_2 \) is the longitudinal strain), that is, in the thickness direction, giving \( s^2 = 1/s_2 \). For small strain (\( e_x \leq 0.2 \)), the strain response \( e_x \) of materials under Maxwell’s compression stress, \( \sigma_M = -e E^2 \), can be approximated as that of a linear elastic material with Young’s modulus (Y): \( e_x = -e E^2 / Y \), where \( E \) is the electrical field and \( e \) is the permittivity. As \( s_x = 1 + e_2 \) and \( f_0 = s^2 \), the relation of focal length with voltage \( V \) is as described in Eq. 3, where \( r \) is the instantaneous thickness of the elastomer, which is a function of the applied voltage but can be approximated as a constant because it changes very little (33). By writing \( b = e/(Yr^2) \), the series expansion for small voltages near \( V = 0 \) gives \( f_0 = 1/(1+bV^2) = 1 + bV^2 + b^2V^4 + O(V^6) \). We see that the focal length transition from a quadratic relation \( (V^2) \) to a quartic relation \( (V^4) \) as the voltage increases: \( V_{\text{transition}} > b^{1/2} \) (and to higher orders if \( V \) increases further). For example, by taking nominal values for our dielectric layer made of VHB (\( e_1 = 6 \), \( Y = 1.8 \) MPa, and \( t = 30 \) μm), \( V_{\text{transition}} \) becomes 5.52 kV.

**Aberrations introduced by stretching**

In tunable systems, optical aberrations may be augmented or reduced by tuning. With metalenses, spherical aberration using normal incidence illumination is corrected by design. However, when such a metasurface is deformed, the resulting aberration is not obvious. The wavefront aberration function or WAF (WAF = \( \phi_{\text{stretched}} - \phi_{\text{ideal}} \)) quantifies the deviation of the resulting phase profile of the stretched metasurface from the ideal phase profile: \( \text{WAF} = \pm k \left( \sqrt{(r/s)^2 + (s f_0)^2} - s f_0 \right) \).

\[
\pm k \left( \sqrt{r^2 + (s f_0)^2} - s f_0 \right) = \pm k \left( \frac{(r/s)^2}{s^2} + f_0^2 - f_0 \right) = \frac{k}{s^2} \left( \frac{r^2}{s^2} + f_0^2 - f_0 \right) + O(r^4).
\]

This equation shows that as the uniform stretch is increased from \( s = 1 \), WAF increases from 0 until it reaches a maximum aberration (fig. S1C) at \( s \approx 1.22 \) (for example, for a lens with \( f = 6 \) mm and \( f_0 = 50 \) mm, the maximum aberration is <0.05 rad at the edge). Upon further stretching, built-in suppression of spherical aberration comes into effect, in which the WAF decays following a quartic function \( (r/s)^4 \). This allows for highly tunable lens devices with excellent immunity to aberration.
Statistical methods
Statistical data were presented with the means plotted and with error bars indicating 1 SD.

SUPPLEMENTARY MATERIALS
Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/4/2/eaap9957/DC1

REFERENCES AND NOTES

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